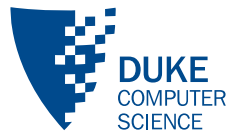


Search

George Konidaris
gdk@cs.duke.edu




Spring 2015

(pictures:Wikipedia)

Search

Basic to problem solving:

- Problem can be in various *states*.
- Start in an *initial state*.
- Have some *actions* available.
- Each action has a *cost*.
- Want to reach some *goal*, minimizing cost.



5	3		7					
6			1	9	5			
	9	8						6
8				6				3
4			8	3				1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9



5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

Happens in simulation.
Not web search.

Formal Definition



Set of states S

Start state $s \in S$

Set of actions A and action rules $a(s) \rightarrow s'$

Goal test $g(s) \rightarrow \{0, 1\}$

Cost function $C(s, a, s') \rightarrow \mathbb{R}^+$

So a search problem is specified by a tuple, (S, s, A, g, C) .

Example

Sudoku


States: all legal Sudoku boards.

Start state: a particular, partially filled-in, board.

Actions: inserting a number into the board.

Goal test: all cells filled and no collisions.

Cost function: 1 per number.



5	3		7					
6			1	9	5			
	9	8						6
8				6				3
4			8	3				1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

Example

Flights - e.g., ITA Software.



States: airports.

Start state: RDU.

Actions: available flights from each airport.

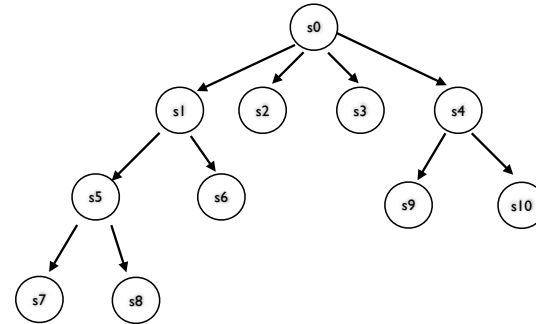
Goal test: reached Tokyo.

Cost function: time and/or money.



The Search Tree

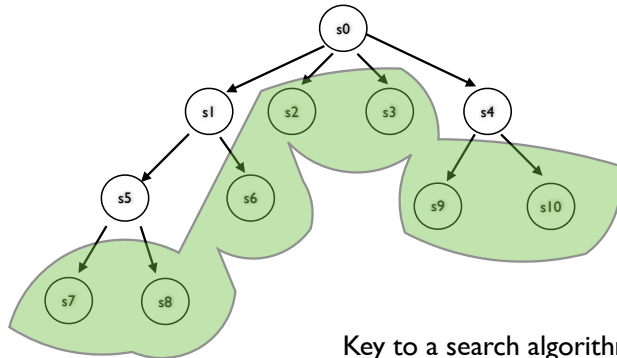
Classical conceptualization of search.



The Search Tree

Expand the tree one node at a time.

Frontier: set of nodes *in tree*, but not *expanded*.



Key to a search algorithm:
which node to expand next?



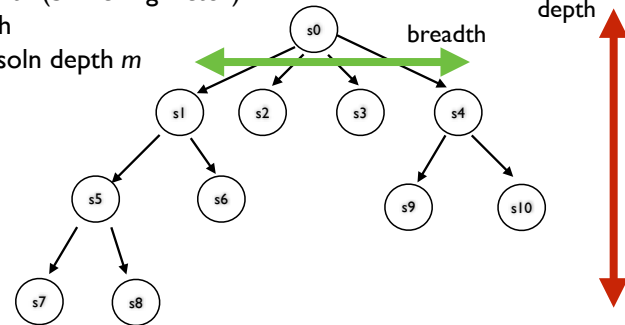
The Search Tree

Important quantities:

breadth (branching factor)

depth

min soln depth m



$O(b^d)$ leaves in a search tree of breadth b , depth d .



How to Expand?



Uninformed strategy: you know nothing about likely solutions in the tree.

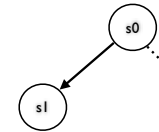
What to do?

- Expand deepest node (*depth-first search*)
- Expand closest node (*breadth-first search*)

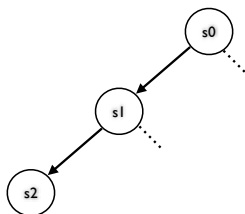
Properties

- Completeness
- Optimality
- Time Complexity (*total number of nodes visited*)
- Space Complexity (*size of frontier*)

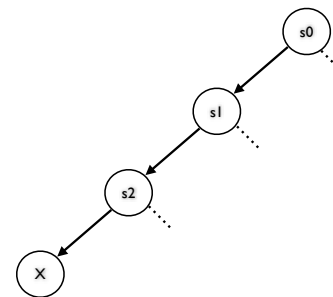
Depth-First Search



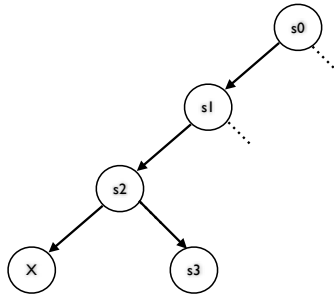
Depth-First Search



Depth-First Search



Depth-First Search



Depth-First Search



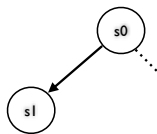
Properties:

- **Completeness:** Only for finite trees.
- **Optimality:** No.
- **Time Complexity:** $O(b^{d+1})$
- **Space Complexity:** $O(bd)$

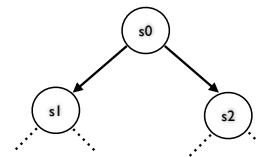
Here m is depth of found solution (*not necessarily min solution depth*).

The deepest node happens to be the one you most recently visited - easy to implement recursively OR manage frontier using LIFO queue.

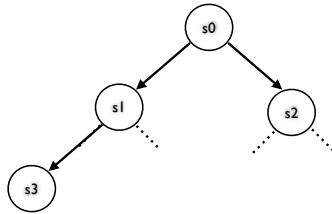
Breadth-First Search



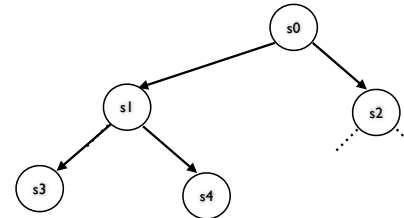
Breadth-First Search



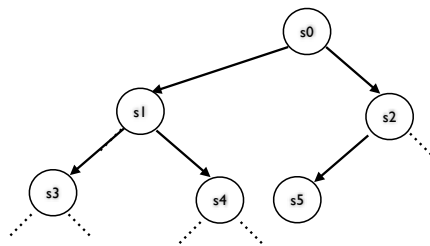
Breadth-First Search



Breadth-First Search



Breadth-First Search



Breadth-First Search



Properties:

- Completeness: Yes.
- Optimality: Yes for constant cost.
- Time Complexity: $O(b^{m+1})$
- Space Complexity: $O(b^{m+1})$

Better than depth-first search in all respects except *memory* cost - must maintain a large frontier.

Manage frontier using FIFO queue.

Iterative Deepening Search



Combine these two strengths.

The core problems in DFS are a) *not optimal*, and b) *not complete*. In both cases, because it fails to explore other alternatives.

Iterative Deepening:

- Run DFS to a fixed depth z .
- Start at $z=1$. If no solution, increment z and rerun.

IDS



Optimal for constant cost! Proof?

How can that be a good idea?
It duplicates work.

Sure but:

- Low memory requirement (equal to DFS).
- Not many more nodes expanded than BFS. (About twice as many for binary tree.)

IDS



Key Insight:

- Many more nodes at depth $m+1$ than at depth m .

MAGIC.

“In general, iterative deepening search is the preferred uninformed search method when the state space is large and the depth of the solution is unknown.” (R&N)

Friday



Informed searches ... what if you know something about the the solution? What form should such knowledge take? How should you use it?

Ponder.